

$V_{A1} = 0V$

$I_{DA1} = -I_{O2} = -1mA$

$I_{DA2} = I_{O1} - I_{O2} = 1mA$

Annahme in ~~Aktive~~ Bereich.
Abschnitt.

für T_1 P-Diode.

~~$U_{AS} < U_{th}$~~

$U_{AS} < U_{AS(th)}$

$U_{AD} > U_{AS(th)}, U_{DS} < 0$

$I_{DA1} = -\frac{\beta}{2} (U_{AS} - U_{th})^2$

$U_{th} = U_{th,0,p} - \left(\sqrt{\phi + U_{BSA1}} - \sqrt{\phi} \right)$

mit $U_{BSA1} = U_{DD} - U_e + U_{ASA1}$

in der Form U_{AS} . ~~ist~~ $U_{AS} < U_{th}$ ist nicht möglich.

$\Rightarrow \frac{-2I_{DA1}}{\beta} = (U_{AS} - U_{th})^2$

$U_{AS} - U_{th} = \pm \sqrt{\frac{2I_{DA1}}{\beta}}$

← $U_{AS} < U_{th}$, ~~ist~~ $U_{AS} < U_{th}$ ist nicht möglich

$U_{AS} = \pm \sqrt{\frac{2I_{DA1}}{\beta}} + U_{th,0,p} - \left(\sqrt{\phi + U_{BSA1}} - \sqrt{\phi} \right)$

$U_{ASA1} = \pm \sqrt{\frac{2I_{DA1}}{\beta}} + U_{th,0,p} - \left(\sqrt{\phi + U_{DD} - U_e + U_{ASA1}} - \sqrt{\phi} \right)$

$\sqrt{\phi + U_{DD} - U_e + U_{ASA1}} = -U_{ASA1} - \left(\sqrt{\frac{2I_{DA1}}{\beta}} + U_{th,0,p} + \sqrt{\phi} \right) \leftarrow [- (U_{ASA1} - U_{th})]^2$

$\sqrt{\phi + U_{DD} - U_e + U_{ASA1}} = U_{ASA1} - U_{th,0,p} - \sqrt{\frac{2I_{DA1}}{\beta}} - \sqrt{\phi}$

$U_{ASA1}^2 + (2U_{th,0,p} + \sqrt{\frac{2I_{DA1}}{\beta}} + \sqrt{\phi}) U_{ASA1} + (U_{th,0,p}^2 + \sqrt{\frac{2I_{DA1}}{\beta}} U_{th,0,p} + \sqrt{\phi} U_{th,0,p} + \phi) = 0$

$\frac{2U_{th,0,p} + \sqrt{\frac{2I_{DA1}}{\beta}} + \sqrt{\phi}}{2} \pm \frac{1}{2} \sqrt{(2U_{th,0,p} + \sqrt{\frac{2I_{DA1}}{\beta}} + \sqrt{\phi})^2 - 4(U_{th,0,p}^2 + \sqrt{\frac{2I_{DA1}}{\beta}} U_{th,0,p} + \sqrt{\phi} U_{th,0,p} + \phi)}$

zuerst $U_{th,0,p}$, $U_{th,0,p} = -\sqrt{\frac{2I_{DA1}}{\beta}} + U_{th,0,p} + \sqrt{\phi} \approx -0.66V$

$-0.33V \pm 0.866V$. $U_{th,0,p} < 0.6V \Rightarrow U_{ASA1} = -1.401V$

für T_2 .

$U_{ASA2} = \sqrt{\frac{2I_{DA2}}{\beta}} + U_{th,0,n} \Rightarrow U_{ASA2} = 1.6V > 0.6V$ nicht gesperrt

$U_{th} = U_{th,0,n} = 0$

$U_{DSA1} = U_{DS} - U_{SA1} = U_{ASA2} - (U_e - U_{ASA1}) = 1.6 - 2 = -1.401V < 0V$

$U_{DSA2} = U_{SA1} = U_e - U_{ASA1} = 3.401V > 0V$

letzter Schritt. ITF-Knoten.

$T_1: U_{AD} > U_{th} \Rightarrow U_{DS} < U_{AS} - U_{th,p} V$

richtig.

$T_2: U_{AD} < U_{th} \Rightarrow U_{DS} > U_{AS} - U_{th,n} V$

$I_{p6} = I_{o2} = I_{D1}$

$I_{D4} = -I_{O1} = I_{p3}$

$\rightarrow U_{AS4} + I_{O2} \cdot R_B + U_{AS1} = U_{DD}$

$U_{AS1} = U_{AS6} = \sqrt{\frac{2I_{DA1}}{\beta}} + U_{th,0,p}$
 $= 1.047V$

$U_{AS4} = U_{AS3} = -\sqrt{\frac{2I_{DA1}}{\beta}} + U_{th,0,p}$
 $= -1.047V$

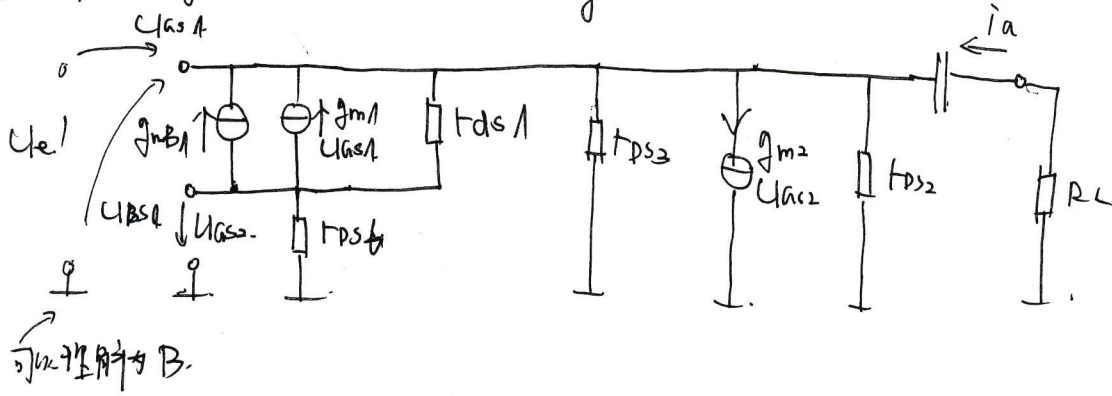
$R_B = \frac{U_{DD} + U_{AS4} - U_{AS1}}{I_{O2}}$

$= \frac{5 - 2.094}{1mA}$

$= 2.906k\Omega$

$M = \frac{I_{O1}}{I_{O2}} = 6$

(2) Kleinsignal-Ersatzschaltung



$$g_{m1} = \sqrt{-2\beta \cdot I_{PA} \cdot (1 - \alpha U_{GS1})} \approx \sqrt{-2\beta \cdot I_{PA}} = 4.4 \text{ mS}$$

$$g_{mB1} = \frac{r \cdot g_m}{2\sqrt{\phi - U_{GS1}}} = 0.77 \text{ mS}$$

$$g_{m2} = \sqrt{2 \cdot \beta \cdot I_{PA2}} = 10 \text{ mS}$$

$$r_{DS1} = \frac{1}{\lambda \cdot I_{PA1}} \approx -\frac{1}{\lambda \cdot I_{PA1}} = 40 \text{ k}\Omega$$

$$r_{DS4} = r_{DS1} = 40 \text{ k}\Omega \quad r_{DS3} \text{ and } r_{DS2} \text{ are not used}$$

Output current i_a

$$i_a = \frac{U_a'}{r_{DS2}} + \frac{U_a'}{r_{DS3}} + g_{m2} U_{GS2} + \frac{U_{GS2}}{r_{DS6}}$$

$$\textcircled{1} i_a' = \frac{U_a'}{r_{DS2}} + \frac{U_a'}{r_{DS3}} + g_{m2} U_{GS2} + \frac{U_{GS2}}{r_{DS6}}$$

$$\textcircled{2} U_{e1} \neq 0, U_{e1} = 0, \rightarrow U_{GS1} = U_{GS1} = -U_a'$$

$$\textcircled{3} U_a' = g_{m1} U_a' (g_{mB1} + g_{m1}) \cdot r_{DS1} + \frac{U_{GS2}}{r_{DS6}} \cdot U_{GS2}$$

$$U_{GS2} + \left[(g_{mB1} + g_{m1}) U_a' + \frac{U_{GS2}}{r_{DS6}} \right] \cdot r_{DS1} \Rightarrow \text{Apply } g_{m1} U_a'$$

| | |
|---------------------|--|
| $\frac{U_a'}{I_a'}$ | $U_{GS2} + U_{GS2} \cdot \frac{r_{DS1}}{r_{DS6}} + r_{DS1} \cdot U_a' (g_{mB1} + g_{m1}) = U_a'$ |
| | $U_a' = \frac{U_{GS2} + U_{GS2} \left(\frac{r_{DS1}}{r_{DS6}} \right)}{1 - r_{DS1} (g_{mB1} + g_{m1})}$ |
| | $I_a' =$ |

$$g_A = \frac{1}{r} = \frac{I_a}{U_a} = \frac{1}{r_{DS2}} + \frac{1}{r_{DS3}} + \frac{g_{m2} U_{GS2} [1 - r_{DS1} (g_{mB1} + g_{m1})]}{U_{GS2} \left[1 + \frac{r_{DS1}}{r_{DS6}} \right]} + \frac{[1 + r_{DS1} (g_{mB1} + g_{m1})]}{r_{DS6} \left[1 + \frac{r_{DS1}}{r_{DS6}} \right]}$$

~~r_{DS2}, r_{DS3}~~

$$r_F = \frac{1}{\frac{1}{r_{DS2}} + \frac{1}{r_{DS3}} + \frac{g_{m2}}{2} [1 - r_{DS1} (g_{mB1} + g_{m1})] + \frac{[1 + r_{DS1} (g_{mB1} + g_{m1})]}{2 r_{DS6}}}$$

$$r_{a'} = \frac{1}{\frac{1}{r_{DS2}} + \frac{1}{r_{DS3}} + (g_{m2} + \frac{1}{r_{DS6}}) \cdot [1 + r_{DS1}(g_{m1} + g_{m2})]}$$

$$\approx \frac{2}{g_{m2}(1 + r_{DS1}(g_{m1} + g_{m2}))}$$

At λ . $r_{a'} \approx \frac{2}{g_{m2} r_{DS1} (g_{m1} + g_{m2})} = 0.742 \text{ [k}\Omega\text{]} \approx 0.7 + 4 \text{ k}\Omega$

ms kV mV

Verstärkung,

$$V' = \frac{U_{a'}}{U_{e'}}$$

(1) $U_{BS1} = -U_{a'}$ $U_{AS1} = U_{e'} - U_{a'}$

$$\left[\frac{U_{a'} - U_{AS1}}{r_{DS1}} + g_{mB1} \cdot U_{a'} - g_{m1}(U_{e'} - U_{a'}) \right] \cdot r_{DS6} = U_{AS2}$$

$$U_{a'} - U_{AS2} + r_{DS6} \cdot g_{mB1} \cdot U_{a'} - r_{DS6} \cdot g_{m1} U_{e'} + \underbrace{g_{m1} U_{a'}}_{r_{DS6} \cdot g_{m1} U_{a'}} = U_{AS2}$$

$$U_{a'} + r_{DS6}(g_{mB1} + g_{m1})U_{a'} - r_{DS6} g_{m1} U_{e'} = 2U_{AS2} \quad (1)$$

$$\frac{U_{AS2}}{r_{DS6}} \neq \frac{U_{a'}}{R_L} + \frac{U_{a'}}{r_{DS2}} + \frac{U_{a'}}{r_{DS3}} + g_{m2} U_{AS2} = 0 \quad (2)$$

$$\Rightarrow U_{AS2} = \frac{-\left[\frac{U_{a'}}{R_L} + \frac{U_{a'}}{r_{DS2}} + \frac{U_{a'}}{r_{DS3}} \right]}{\frac{1}{r_{DS6}} + g_{m2}}$$

$$+ r_{DS6} g_{m1}$$

$$\frac{+ r_{DS6} g_{m1}}{+ r_{DS6}(g_{mB1} + g_{m1}) + \frac{2 \left[\frac{1}{R_L} + \frac{1}{r_{DS2}} + \frac{1}{r_{DS3}} \right]}{\frac{1}{r_{DS6}} + g_{m2}}} = V' \quad \uparrow \quad 0.84$$

或于负载电阻对增益的影响

VG-02.

Vorlesung 2 内容整理:

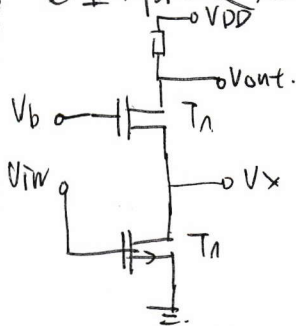
- $U_{DS} + U_{GS} = U_{th} \rightarrow U_{GS} = U_{th}$

$U_{GS} = U_{GS2} + U_{GS4}$; $U_{DS2, sat} = U_{GS} - U_{th} = \sqrt{\frac{2I_0}{\beta}}$

$U_{DS2} = -U_{GS4} + U_{GS3} + U_{GS1} = -U_{GS4} + U_{GS3} + U_{GS2}$

$U_{GS3} = U_{GS4} \Rightarrow U_{DS2} = U_{GS2}$

这里取两个管子为源一共栅电路



要让两个管子都工作在饱和区

即 $V_x \geq V_{in} - V_{th1}$, $V_x = V_b - U_{GS2} \Rightarrow V_b \geq V_{in} - V_{th1} + U_{GS2}$

$V_{out} \geq V_b - V_{th2} \Rightarrow V_{out} \geq V_{th1} - V_{th2} + U_{GS2} - V_{th1}$

在饱和区: $I_{D2} = \frac{\Delta U_{GS}}{I_{D3} + I_{D4}} I_{D3}$

所以认为 $I_{D1} = I_{D2}$. 又 $I_{D3} = I_{D4} \Rightarrow U_{GS3} = U_{GS4}$

$U_{DS4, min} = U_{DS4, sat} = \sqrt{\frac{2I_0}{\beta}} = 0.31V$

$U_{GS, min} = U_{GS} + U_{DS4, min} = U_{GS2} + U_{DS4, min} = U_{DS2, sat} + U_{th} + U_{DS4, min}$

$= \sqrt{\frac{2I_0}{\beta}} + U_{th} + U_{th} = 1.23V$

$U_{DS1} \geq U_{GS1} - U_{th} \rightarrow U_{GS1} \leq U_{DS1} + U_{th} \leq U_{DS1} + U_{DS3} + U_{th}$

$\Rightarrow I_{ref} = \frac{I_0}{J} \Rightarrow \beta_J = \frac{\beta}{20}$. 由 β 和 β_J 关系控制电流

(1) $U_{GS, min} = U_{DS2, sat} + U_{DS4, sat} = 2 \cdot U_{DS, sat} = 0.4V$ $U_{DS3} \neq U_{DS4}$

$U_{GS1} - U_{th} = U_{DS, sat} \Rightarrow U_{GS1} = U_{DS, sat} + U_{th} = 0.8V$

$U_{GS1} = U_{GS3} = 1.4 = U_{GS1} + U_{DS, sat} = 0.8 + 0.2 = 1.0V$

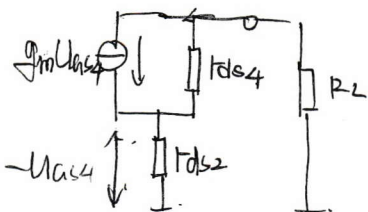
$R_D = \frac{U_{GS3} - U_{GS1}}{I_0} = \frac{U_{DS, sat}}{I_0} = \frac{0.2}{1 \times 10^{-4}} = 2 \times 10^3 = 2k\Omega$

$\beta = J$

$R_0 = \frac{U_{GS3} - U_{GS1}}{I_0} = \frac{0.2}{1 \times 10^{-4}} = 2k\Omega$

$U_{GS3} - U_{GS1} = \frac{2}{1 \times 10^{-4}} = 20k\Omega \Rightarrow R = R_0 + R_D = 22k\Omega$

(2) 共源-共栅电路



$I_n = \frac{2I_0}{\beta} \sqrt{2\beta I_{DA}} = \sqrt{2 \cdot J \cdot 0.1} = 1mA$

$t_{DS} = \frac{C_{ds} + C_{gs4}}{I_{DA}} \approx \frac{1}{\lambda I_{DA}} \approx 20k\Omega$

$-\frac{g_{m4} U_{gs4}}{t_{ds2}} = i_o$

$(-\frac{U_{GS4}}{t_{ds2}} - g_m U_{GS4}) t_{ds4} \approx U_{GS4} = i_o$

$\Rightarrow -(g_m t_{ds4} + 2) U_{GS4} = i_o \Rightarrow t_o = t_{ds2} (g_m t_{ds4} + 2) \approx 62 \mu s$

$$(3) U_{GS}(T) = \sqrt{\frac{2I_D}{\beta}} + U_{th}$$

$$\frac{\partial U_{GS}}{\partial T} \Big|_{T=T_0} = \frac{\partial I_D}{\partial T} \Big|_{T=T_0} + \frac{\partial U_{th}}{\partial T} \Big|_{T=T_0}$$

$$\frac{\partial U_{GS}(T)}{\partial I_D} \Big|_{T=T_0} \cdot \frac{\partial I_D}{\partial T} \Big|_{T=T_0} + \frac{\partial U_{th}}{\partial T} \Big|_{T=T_0}$$

$$\frac{\partial U_{GS}(T)}{\partial \beta} \Big|_{T=T_0} \cdot \frac{\partial \beta}{\partial T} \Big|_{T=T_0} + \frac{\partial U_{th}}{\partial T} \Big|_{T=T_0}$$

$$\frac{\partial U_{GS}(T)}{\partial U_{th}} \Big|_{T=T_0} \cdot \frac{\partial U_{th}}{\partial T} \Big|_{T=T_0} + \frac{\partial U_{th}}{\partial T} \Big|_{T=T_0}$$

$I_D = I_0 = \text{konst.}$

$$\frac{\partial U_{GS}(T)}{\partial \beta} = \frac{-\partial I_D \cdot \frac{1}{\beta^2}}{2 \sqrt{\frac{2I_D}{\beta}}} \Big|_{T=T_0} = -\frac{\sqrt{2I_D}}{\beta^2 \sqrt{\frac{2}{\beta I_D}}}$$

$$\frac{\partial \beta}{\partial T} \Big|_{T=T_0} = \frac{\beta_0}{T_0} \cdot \left(-\frac{3}{2} \sqrt{\frac{T}{T_0}}\right)^{-\frac{1}{2}} = -\frac{3}{2} \frac{\beta_0}{T_0}$$

$$\frac{\partial U_{GS}}{\partial U_{th}} \Big|_{T=T_0} = 1, \quad \frac{\partial U_{th}}{\partial T_0} \Big|_{T_0} = -1.1 \text{ mV/K}$$

$$\Rightarrow -\frac{3}{2} \frac{\beta_0}{T_0} \cdot \frac{\partial \sqrt{2I_D}}{\partial \beta} = +\frac{3}{4T_0} \sqrt{\frac{2I_D}{\beta_0}}$$

$$\frac{\partial U_{GS}}{\partial T} \Big|_{T=T_0} = \frac{3}{4T_0} \sqrt{\frac{2I_D}{\beta_0}} - 1.1 \frac{\text{mV}}{\text{K}} = -0.5 \text{ mV/K}$$

